

Deductive Databases & Knowledge Based Systems

Sheet 6 (until 12.05.2008)

Exercise 1

1. What is a least Herbrand model? (1p)
2. What are minimal Herbrand models? (1p)
3. What are perfect Herbrand models? (1p)
4. In general, why aren't there least Herbrand models for $Datalog^{neg}$? (1p)

Exercise 2

Provided is following $Datalog^f$ program:

$edge(3,2).$
 $edge(2,6).$
 $edge(2,5).$
 $edge(5,3).$
 $path(X,Y) : - edge(X,Y).$
 $path(X,Y) : - edge(X,Z), path(Z,Y).$

Compute the least model step by step using the fixpoint iteration. (4p)

Exercise 3

Provided is following $Datalog^{neg}$ program:

$q(1,2).$
 $q(2,3).$
 $s(1,3).$
 $r(X,Y) : - s(X,Y).$
 $p(X,Y) : - q(X,Y), \neg r(X,Y).$
 $p(X,Y) : - q(X,Y), \neg s(X,Y).$
 $p(X,Y) : - p(X,Y), p(X,Y).$

1. Provide all minimal Herbrand models of the program. (2p)
2. Provide a program connection graph and stratification for the program. (2p)
3. Partition the program according the stratification into $\mathcal{P} := \mathcal{P}_0 \cup \dots \cup \mathcal{P}_0$ (1p)
4. Compute the perfect model step by step using the iterated fixpoint iteration. (4p)
5. $Datalog^f$ is supposed to be computationally complete. Thus, the above program should be able to be expressed in $Datalog^f$. Provide an equivalent version of the program without negation. (3p)